Nonequilibrium Mass Transport in the 1D Fermi-Hubbard Model

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We experimentally and numerically investigate the sudden expansion of fermions in a homogeneous one-dimensional optical lattice. For initial states with an appreciable amount of doublons, we observe a dynamical phase separation between rapidly expanding singlons and slow doublons remaining in the trap center, realizing the key aspect of fermionic quantum distillation in the strongly interacting limit. For initial states without doublons, we find a reduced interaction dependence of the asymptotic expansion speed compared to bosons, which is explained by the interaction energy produced in the quench.

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Many-body physics in one dimension (1D) differs in numerous essential aspects from its higher-dimensional counterparts. Several familiar concepts, such as Fermi-liquid theory [1,2], are not applicable in 1D. Moreover, many 1D models are integrable, meaning that there exist exact solutions. Examples include the Lieb-Liniger model [3], the Heisenberg chain [4], or the 1D Fermi-Hubbard model (FHM) [5]. These models exhibit extensive sets of conserved quantities that prevent thermalization [6–11] and can, in lattice systems, lead to anomalous transport properties [12–15]. Cold-atom experiments offer the possibility to study transport properties of strongly correlated quantum gases in a clean environment. Their excellent controllability enabled far-from-equilibrium experiments [16–20] as well as close-to-equilibrium measurements in the linear-response regime [21–24] both in extended lattices and mesoscopic systems [25–27].

Here, we investigate mass transport in the 1D FHM in far-from-equilibrium expansion experiments [18–20], where an initially trapped gas is suddenly released into a homogeneous potential landscape as illustrated in Fig. 1. There are two distinct regimes of interest in sudden-expansion studies: the asymptotic one, where the expanding gas has become dilute and effectively noninteracting [28–36] and the transient regime, where the dynamical quasicondensation of hardcore bosons [37–41] and quantum distillation [20,42–44] have been found.

Quantum distillation occurs for large interactions. It relies on the dynamical demixing of fast singlons (one atom per site) and slow doublons (two atoms per site)
during the expansion: while isolated doublons only move with a small effective second-order tunneling matrix element $J_{\text{eff}} = 2J^2 / U \ll J$ for $U \gg J$ [45,46], neighboring singlons and doublons can exchange their positions via fast, resonant first-order tunneling processes. Thus, after opening the trap, singlons escape from regions of the cloud initially occupied by singlons and doublons, leading to a spatial separation of the two components. Without an increase of the doublon density in the central region, this regime is termed weak quantum distillation [44]. Ideal initial-state conditions can lead to a strong version of quantum distillation, where the spatial separation of singlons and doublons yields a contraction of the doublon cloud radius [Fig. 1(a)]. In the extreme limit this distillation could be used to purify a finite-temperature band insulator [42], thereby dynamically generating low-entropy regions. This would represent a major advancement in the ongoing quest of realizing fermionic many-body physics at the lowest entropy scales [47–51]. So far, experimental evidence for weak quantum distillation has only been found for bosons [20] at intermediate interaction strengths, where doublons can decay into singlons on time scales relevant to quantum distillation.

In this work, we investigate the nonequilibrium mass transport in the 1D FHM starting from initial product states in deep optical lattices [18,19], while close-to-thermal initial states were used in Ref. [20]. The expansion dynamics is initiated by two simultaneous quenches: a sudden increase of the tunnel coupling, resulting in a quench from almost infinite to finite $U/J$, and a sudden removal of the harmonic trap (Fig. 1). We prepare initial product states with or without doublons (Fig. 1) and quantitatively investigate the time evolution of singlon and doublon densities individually. For initial states with doublons, we find a distinct dynamical phase separation between singlons and doublons, which is the fundamental mechanism of fermionic quantum distillation [Fig. 1(a)]. For initial states without doublons [Fig. 1(b)], we study interaction effects in the asymptotic expansion velocities [35]. We observe that the cloud expands rapidly at all interaction strengths with slightly smaller velocities at intermediate values, in agreement with our numerical simulations. This can be interpreted in terms of the interaction energy produced in the quench of $U/J$, which leads to the dynamical formation of doublons [19,33,52].

**Experiment.**—We prepare a degenerate Fermi gas of $30(1) \times 10^3$ 40K atoms in a crossed dipole trap at the initial temperature $T/T_F = 0.15(1)$, where $T_F$ is the Fermi temperature. The gas consists of an equal mixture of two spin components corresponding to the states $|\uparrow\rangle = |m_F = -7/2\rangle$ and $|\downarrow\rangle = |m_F = -9/2\rangle$ in the $F = 9/2$ hyperfine ground-state manifold. Our sequence begins with loading the atoms into a blue-detuned three-dimensional optical lattice with wavelength $\lambda_\perp = 532$ nm and lattice constant $d = \lambda_\perp / 2$ along the $x$ direction and $\lambda_\parallel = 738$ nm in the transverse directions. While the main lattice along $x$ is initially loaded to 20 $E_{rx}$, the transverse lattices are simultaneously ramped to a depth of $33E_{rx}$, where they remain during the whole sequence to realize individual 1D systems. Here, $E_{ij} = \hbar^2k_j^2/(2m)$ are the respective recoil energies with $j \in \{x, \perp\}$, $k_j = 2\pi/\lambda_j$ denotes the corresponding wave vector, and $m$ is the mass of $^{40}$K. Holding the atoms in the deep initial lattice for 20 ms dephases remaining correlations between neighboring sites, such that the resulting state can be approximated as a product state $|\psi_0\rangle = \prod_{i\in\text{trap}} (\hat{c}_{i\sigma}^{\dagger})^{n_i} (\hat{c}_{i\sigma})^{n_i^\dagger}|0\rangle$, where $\hat{c}_{i\sigma}^{\dagger}$ is the fermionic creation operator, $n_{i\sigma} \in \{0,1\}$, $\sigma \in \{\uparrow,\downarrow\}$, and $i$ is the lattice-site index. The spin orientations are expected to be distributed randomly among the sites and the average number of atoms per lattice site in the center of the cloud $\langle \hat{n}_i \rangle = \sum_\sigma \langle \hat{n}_{i\sigma} \rangle$ is estimated to be $\langle \hat{n}_i \rangle \lesssim 0.9$ [53], $\hat{n}_{i\sigma} = \hat{c}_{i\sigma}^{\dagger}\hat{c}_{i\sigma}$ is the density operator. The fraction of atoms on doubly occupied sites $n_d = N_d/(N_s + N_d)$ in the initial state can be tuned via the interaction strength during the loading process employing a Feshbach resonance at 202.1 G [53]. Here, $N_s(N_d)$ denotes the number of particles on singly (doubly) occupied sites. The dynamics starts with suddenly quenching the main lattice to 8 $E_{rx}$. Simultaneously, the strength of the dipole trap is adjusted to compensate the anticonfining harmonic potential introduced by the lattice [53]. Our system is then described by the homogeneous 1D FHM

$$\hat{H} = -J \sum_{i,\sigma = \uparrow, \downarrow} (\hat{c}_{i\sigma}^{\dagger}\hat{c}_{i+1\sigma} + \text{H.c.}) + U \sum_i \hat{n}_i \hat{n}_{i\uparrow}. \quad (1)$$

After a variable expansion time $t$ the on-site population is frozen by suddenly increasing the lattice depth to 20 $E_{rx}$. Subsequently, the cloud is imaged in situ using high-field imaging either with or without removing doublons [53]. By combining these images, the dynamics of singlons and doublons can be resolved individually.

**Quantum distillation.**—We characterize the dynamics by monitoring the singlon and doublon clouds as a function of the expansion time for an initial state with $n_d = 0.40(2)$ [Figs. 2(a), 2(b)]. Isolated doublons are expected to become stable objects for interaction strengths that are large compared to the bandwidth $U \gg W$, $W = 4J$ [63], since in this case the interaction energy released in the doublon decay cannot be transferred into kinetic energy of singlons in low-order processes [45,63]. This is in agreement with our observations [insets in Figs. 2(a), 2(b)], where for $U = 5J$ we witness a fast doublon decay of about 25% in the early stages of the expansion $t \lesssim 5r$, which is accompanied by a compatible increase of the singlon number. In contrast, both numbers remain approximately constant for $U = 20J$. Except for a small residual decay, which is attributed to light-assisted losses of doublons [64], this enables us to probe the dynamical phase separation of singlons and doublons at approximately constant doublon numbers.
We study the phase separation by extracting the cloud sizes \( R_s; d; d \) (\( t \)) at half-width-at-half maximum (HWHM). We observe a rapidly expanding singlon cloud, which has approximately doubled in size at \( t = 40 \tau \). In contrast, the doublon cloud size grows much slower and we even observe a weak shrinking of the cloud for \( U = 20 J \). For comparison, we show the expected expansion of a fictitious cloud of noninteracting doublons expanding according to \( J_{\text{eff}} \) [53]. The difference highlights the nontrivial nature of this transient dynamics. The dynamical phase separation is even more evident in the comparison of the integrated line densities of singlon and doublon clouds at \( t = 0 \) and \( t = 40 \tau \) for our strongest interactions [Fig. 2(c)]. Clearly, the singlons expand significantly, while the doublons essentially remain in the center of the cloud. As a consequence, the ratio of atom numbers on doubly and singly occupied sites \( N_c^d/N_c^s \) in the center of the cloud increases by about 40% [Fig. 2(d)]. While this signal could in principle be caused by 1D systems with a low doublon fraction, a quantitative analysis based on our measured initial density distributions shows that their contribution to the signal is negligible [53]. Hence, our data establish clear evidence for fermionic quantum distillation in the weak regime in a nonequilibrium mass-transport experiment.

**tDMRG results for transient dynamics.**—Quantum distillation in the strong regime can further lead to a shrinking of the doublon cloud. The precise amount depends on the number of singlons initially confined in the doublon cloud, the initial density, and the cloud size [42,44,53]. Here, we focus on the role of the initial density, which has the largest influence. Figure 3 shows tDMRG simulations of the relative change of the doublon cloud size \( \Delta R_d(t) = R_d(t)/R_d(0) - 1 \) as a function of time for different average initial densities \( n = (N_s + N_d)/L_{\text{init}} \) in an ideal box trap of length \( L_{\text{init}} \) for constant \( n_d = 0.4 \) [53]. Negative values of \( \Delta R_d \) indicate a shrinking of the doublon cloud, while \( \Delta R_d > 0 \) corresponds to an expanding doublon cloud. For the initial state with the largest density \( n = 1.25 \), the doublon cloud shrinks significantly, while for \( n = 0.83 \), the cloud expands only slightly. Inset: Experimental data for \( \Delta R_d \) as a function of the interaction strength at \( t = 40 \tau \) for constant initial density of \( n_d = 0.4 \). The solid line represents the linear fit to the experimental data [53].

**FIG. 2.** Dynamical phase separation of singlons and doublons. Half-width-at-half-maximum (HWHM) size \( R_s;d; d \) of singlon (\( s \), red) and doublon (\( d \), blue) clouds as a function of time for (a) \( U = 5J \) and (b) \( U = 20J \). The dashed lines illustrate the hypothetical expansion of a noninteracting doublon cloud with effective tunneling \( J_{\text{eff}} \) [53]. Insets: Number of atoms on singly and doubly occupied sites, \( N_s \) and \( N_d \), as a function of time. (c) Experimental snapshots of the integrated line densities of singlon and doublon clouds, \( \rho_s(x) \) and \( \rho_d(x) \), at \( t = 0 \) (left) and \( t = 40 \tau \) (right). (d) Ratio \( N_s^d/N_s^s \) of atom numbers on doubly and singly occupied sites in the central region of the cloud (red rectangle in the inset) as a function of time for \( U = 20J \). Every data point is averaged over four measurements and error bars represent the standard error of the mean. Solid lines are guides to the eye.

**FIG. 3.** tDMRG results for the relative doublon cloud size. Main panel: Relative doublon cloud size \( \Delta R_d(t) \) for three different initial uniform densities \( n = (N_s + N_d)/L_{\text{init}} \) in an ideal box trap of length \( L_{\text{init}} \) for constant \( n_d = 0.4 \) [53]. The solid lines end at time \( t_{\text{max}} \), when the width of the singlon cloud increased to \( \Delta R_s = 0.8 \). This value corresponds to the experimental one at \( t = 40 \tau \). Inset: Experimental data for \( \Delta R_d \) as a function of the interaction strength at \( t = 40 \tau \), which was evaluated using linear fits to the time traces \( R_d(t) \) as shown in Figs. 2(a), 2(b) [53].
$n = 1.25$, we observe a large decrease of $\Delta R_d(t)$. This effect is substantially reduced for smaller densities (Fig. 3) due to the presence of holons (empty sites), which remain trapped between doublons on the time scales of the quantum distillation process [44]. Additionally, the dynamics becomes slower, both due to holons and due to the larger cloud sizes used for simulations with smaller average densities [44]. Despite these quantitative differences, however, we find that the fundamental aspect of quantum distillation, i.e., the dynamical phase separation of singlons and doublons, is generally robust.

For comparison, we show the experimentally measured relative changes $\Delta R_d$ as a function of interaction strength [inset in Fig. 3]. For all interactions the time traces of the doublon HWHM are fitted with a linear function to calculate $\Delta R_d$ at the maximum expansion time $t = 40\tau$ [33]. We observe that $\Delta R_d(40\tau)$ approaches zero with increasing interaction strength and becomes slightly negative at $U/J = 20$. In order to facilitate a comparison between experiment and numerics, where much smaller particle numbers are used, we define a time $t_{\text{max}}$ for the simulation at which the relative singlon cloud size $\Delta R_s$ has reached the same value as in the experiment (Fig. 3). Our numerical results indicate that the contraction is not completed at this time. In the experiment this time is limited by the degree of flatness of the homogeneous potential. The remaining difference between the numerical and experimental results is most likely due to other initial-state properties, such as inhomogeneous density distributions and the averaging over several 1D systems with different initial-state properties [33].

**Asymptotic dynamics and interaction effects.**—Here, we focus on the dynamics of the whole cloud for initial states with a negligible doublon fraction ($n_d < 0.05$). We extract the second moment $r^2 = \sum_i (\hat{n}_i - i)^2 d_i^2/(N_\uparrow + N_d)$ of the time-dependent density distribution (see Ref. [33] for details on the analysis), which is routinely computed in numerical simulations [32,33,35]; here $i_0$ is the center of mass of the initially trapped gas. From the time dependence of $r^2$, we extract the asymptotic radial velocity $v_r$ by fitting $\sqrt{r^2} = \sqrt{r^2_0 + v_r^2 \tau}$, where $r_0$ is the initial size of the cloud [33]. Figure 4 shows $v_r$ as a function of $U/J$. We find $v_r = 1.40(6)d/\tau$ for $U = 0$ and $U = 20J$, whereas for intermediate interactions $U \sim 3J$, the radial velocity decreases weakly. Note that for $U \gg W$, the mass transport in the 1D FHM in the absence of doublons becomes identical to a noninteracting gas of spinless fermions and thus behaves exactly like hardcore bosons in 1D with $v_r = \sqrt{2d}/\tau$ [19]. The values in the limiting cases agree with these theoretical predictions for free fermions expanding from our initial state. Remarkably, compared to the Bose-Hubbard model [19], the reduction of $v_r$ at intermediate interaction strengths is much weaker (Fig. 4).

Starting from the limit of very strong interactions, the interaction dependence of $v_r$ can be understood in a two-component picture of independent singlon and doublon gases [65,66]: The dynamically generated doublons undergo a quantum distillation mechanism and are then inert on the time scales of the experiment. Thus, the more doublons are generated, the less kinetic energy is available for the rapidly expanding singlons. Focusing on the quantitative difference between the $v_r(U)$ curves for bosons and fermions, which is the main result of the data presented in Fig. 4, two aspects are important. First, in the case of fermions, doublons can only be generated between sites with fermions of different spin orientation [33]. The initial state that has the most of such $\uparrow - \downarrow$ neighbors is the Néel state, and this initial state leads to the most pronounced minimum of $v_r$ (Fig. 4, [33]). In order to compare to the experiment, we average over many 1D systems with random spin orientations for a balanced spin mixture (dark red diamonds in Fig. 4). This averaging leads to a weaker minimum in $v_r$ than for the Néel state and is in agreement with our experimental data. The second reason for the stronger minimum in $v_r$ for bosons is the fact that the interaction energy can become much larger, since larger local occupancies are possible [19]. In order to test whether the observed $v_r$ can primarily be understood as a function of the interaction energy in the system after the formation of doublons, we show data for different $U/J$ and different spin configurations versus interaction energy in the Supplemental Material (Fig. S8 in Ref. [33]). The data for bosons lie well outside the accessible range of interaction energies for fermions because of higher site occupations, but fall onto an extrapolation of the fermionic data. Hence, the integrability of the 1D FHM does not seem to be the dominant reason for the differences to the bosonic case. An interesting
extension would be the calculation of expansion velocities by exploiting the integrability along the lines of Refs. [35,67], which we leave for future work.

**Summary and outlook.**—We investigated the sudden expansion of an interacting cloud of fermions. Starting from an initial product state with an appreciable doublon fraction, we observed a dynamical phase separation between singlons and doublons, theoretically known as fermionic quantum distillation in the weak regime. Additionally, we analyzed radial velocities for different interaction strengths using initial states consisting purely of singlons. We found a decrease of the radial velocities at weak interactions and attributed this effect to dynamically generated doublons. The weak decrease of radial velocities of expanding fermions compared to bosons is due to the Pauli principle leading to a crucial dependence of the radial velocities on the initial spin configuration. Future experiments could use the singlon and doublon resolved scheme to detect signatures of FFLO states [67–69] in sudden-expansion experiments. Moreover, it would be intriguing to observe the strong localization, J. Stat. Mech. Theor. Exp. 2016 064010.

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[53] See the Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.121.130402, which includes Refs. [54–62], not cited in the main text, for details on the initial state preparation, the creation of a flat potential, the control of the doublon fraction, the singlon-doublon resolved read-out, the estimation of tubes with few doublons, the fits to the time traces of $R_d$, as well as the extraction of the radial velocities. Additionally, details of the tDMRG simulations are explained.
