A Bayesian Network Approach for Coastal Risk Analysis and Decision Making

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Abstract

Emergency management and long-term planning in coastal areas depend on detailed assessments (meter scale) of flood and erosion risks. Typically, models of the risk chain are fragmented into smaller parts, because the physical processes involved are very complex and consequences can be diverse. We developed a Bayesian network (BN) approach to integrate the separate models. An important contribution is the learning algorithm for the BN. As input data, we used hindcast and synthetic extreme event scenarios, information on land use and vulnerability relationships (e.g., depth-damage curves). As part of the RISC-KIT (Resilience-Increasing Strategies for Coasts toolKIT) project, we successfully tested the approach and algorithm in a range of morphological settings. We also showed that it is possible to include hazards from different origins, such as marine and riverine sources. In this article, we describe the application to the town of Wells-next-the-Sea, Norfolk, UK, which is vulnerable to storm surges. For any storm input scenario, the BN estimated the percentage of affected receptors in different zones of the site by predicting their hazards and damages. As receptor types, we considered people, residential and commercial properties, and a saltmarsh ecosystem. Additionally, the BN displays the outcome of different disaster risk reduction (DRR) measures. Because the model integrates the entire risk chain with DRR measures and predicts in real-time, it is useful for decision support in risk management of coastal areas.

Keywords: Natural hazards, disaster risk reduction, southern North Sea, source-pathway-receptor concept

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1. Introduction

About 10% of the world’s population lives in low-lying coastal areas, where they are vulnerable to extreme events generated by the combined impact of waves, surges and tides [1]. For example, if the sea surface elevation is higher than a coastal defense, water overtops or overflows the structure and floods the hinterland. Moreover, engineered flood defenses may fail catastrophically under extreme loading conditions [4, 5]. Similarly, beach and dune erosion at sandy coasts can threaten structures close to the shoreline or result in breaches and inundation [6, 7]. As a consequence, coastal communities may suffer from material damages, economic, political and social disruption, health issues, or damaged ecosystems [8].

Under extreme circumstances, coastal storms can lead to societal disasters. For example, around 1100 lives were lost when Hurricane Katrina made landfall in New Orleans in 2005 [9]. More recently, 47 people died in La Faute-sur-Mer, France, during storm Xynthia in 2010 [10]. These events emphasize a continuing need for effective coastal risk management; this is all the more important as risks are projected to increase globally, due to growing populations and assets, accelerated sea level rise and potential increases in storminess (both tropical and extra-tropical) [11].

Coastal risk management essentially includes two types of activities: taking prompt actions in the face of an impending storm and long-term planning. Accordingly, we distinguish between a hot phase and a cold phase. In the hot phase, emergency managers depend on real-time and reliable predictions of the expected conditions in the coastal zone, as they attempt to select mitigation measures and allocate limited resources minimizing the total sum of negative impacts. In the cold phase, multiple actors, including politicians, local stakeholders and scientists, cooperate to determine sensible strategies for reducing risks in an uncertain future [12]. To evaluate these strategies against historical and conceivable future storms, they turn to impact assessments of the various scenarios.

Cutting across numerous disciplines, including oceanography, coastal science and engineering, statistics, economics, and social and political science, coastal risk assessment is highly challenging. Each field has complex models which target individual elements of the risk process. For example, multivariate probability models estimate the return periods of extreme storms [13, 14], while numerical models, based on, for instance, hydro- and morphodynamic processes, determine the respective natural responses of the coast and extent of flooding [15, 16, 17, 18]. Finally, behavioral or statistical models estimate the diverse and complex consequences onshore [19, 20, 21]. However, risk management requires a framework that integrates the individual elements of the risk process [22].

Two primary issues arise when attempting to incorporate offshore sea conditions with their expected onshore hazards and impacts into a single model for operational use. Numerical models, being computationally expensive, often have a long run time, while instant assessments are needed for any conceivable
hazard scenario during both the hot and cold management phases. On the other hand, the spatial and temporal scales of numerical and impact models differ from one another and need to be integrated. Whereas numerical models have grids whose sizes depend on the physical properties of the area under consideration, impact models usually operate on the level of individual receptors.

In the Netherlands, Jonkman et al. [8] assessed the flood hazard and corresponding damages to the built environment, loss of life, as well as indirect economic impacts (e.g., the interruption of production flows) for one hypothetical extreme event. The fundamental element of this approach is a spatial database through which they connect output and input of the individual models according to a common spatial attribute. While addressing the challenges of different scales, the approach was limited to a single storm scenario. In principle, other storms could be assessed similarly, but the computational time is determined by the underlying numerical models. For this reason, the approach may not be suitable to predict flood hazards and damages for an impending storm or to compare multiple hypothetical storm scenarios during round-table discussions of stakeholders.

In contrast, Poelhekke et al. [23] integrated a wide range of simulated storm scenarios in a discrete Bayesian network (BN) and assessed related onshore hazards in Praia de Faro, Portugal. A BN is a graphical model that describes system relations in probabilistic terms and can give instantaneous predictions. Nevertheless, Poelhekke’s approach did not estimate impacts nor does it provide insight into the effectiveness of risk reduction measures. As far as we know, no model has been proposed which renders instant assessments for various possible storm scenarios and captures the entire risk chain from sea conditions to onshore impacts.

In this article, we design a decision support system (DSS) for the hot and cold phases of coastal risk management as a BN. We build on the widely recognized source-pathway-receptor (SPR) concept and attempt to extend and generalize the work of Poelhekke et al. [23]. The DSS is part of a suite of tools, developed in the RISC-KIT project, whose purpose is to help effective disaster risk reduction (DRR) management at coasts [24]. For different extreme event scenarios, the BN predicts percentages of affected receptors in terms of the hazards experienced and their impacts in real-time. Moreover, the BN can evaluate the effects of potential DRR measures. Although our focus is on marine storms, which are the primary threat to coastline stability, the approach is broader. It is also possible to include, or even solely concentrate on, other types of natural disasters, such as extreme river discharges or exceptional rainfall events in this model.

The remainder of the paper is organized as follows. In Section 2, we introduce the methodological background. We explain the SPR-concept and provide the basic theory of discrete BNs. In Section 3, we describe the design of the DSS, followed by examples from the case study site of Wells-next-the-Sea, Norfolk, UK, in Section 4. Finally, in Section 5, we discuss limitations and potential of the approach and, in Section 6, we present our conclusions.
2. Methodological Background

In this section we provide an overview of models for the different elements in the risk chain, following the logic of the source-pathway-receptor concept, as well as an approach to quantitatively assess the effect of DRR measures. After that we describe the method we use to integrate the various models and DRR measures: BNs.

2.1. The Source-Pathway-Receptor concept

The source-pathway-receptor (SPR) concept is a high-level framework to evaluate risks. It was first used to describe the possible movements of a pollutant from its source to a receptor [25] and is now well established in coastal risk management [26, 27, 28, 29].

In its basic form, the framework characterizes a causal chain of processes and events in terms of sources, pathways and receptors (Figure 1). When considering coastal storms, the chain reaches from offshore to onshore. The source is the offshore marine environment. Typical source variables, or boundary conditions, are peak water level, maximum wave height and peak period, and storm duration. The storm threat can affect onshore areas through pathways. They are the interaction of water levels and waves with coastal landforms and ecosystems, coastal infrastructure and low-lying coastal hinterlands. Finally, receptors are the entities at risk, such as people, built environments or ecosystems.

![Figure 1: Illustration of the source-pathway-receptor (SPR) concept for coastal storms](image)

Sometimes, the framework explicitly includes consequences (C) as a fourth term. Any receptor can experience them, if affected by a hazard. Gouldby and Samuels [30] have defined a hazard as the triple: source, pathway and receptor. However, we consider a hazard to be a local condition directly affecting the receptors. Examples are flood depth, flow velocity and erosion, which can, for instance, cause structural damage or injuries.

Coastal risk assessments often follow this concept. The general idea is to generate a set of representative extreme event scenarios, model the pathways, and estimate the resultant impact [e.g., 31]. More specifically, detailed and specific models are applied to various individual processes in the SPRC chain and then linked together. However, to the best of our knowledge, a single model that captures the entire chain does not exist yet.
2.1.1. Source Models

A set of scenarios that are representative for the storm climate at a given site can be derived from a statistical analysis. Often, storms are characterized by the values of hydraulic variables in deep water at the peak of the storm along with its duration. In the past decade, copula-based models have become increasingly popular to estimate dependencies between (some) such variables [e.g., 13, 32, 33, 14]. Copula models are a specific type of probability distribution that characterizes the dependence structure between random variables irrespective of their marginal behavior. The temporal evolution of the variables, which is typically required as input for pathway models, is often idealized as a so-called equivalent triangle [34]. Nonetheless, a couple of studies model times series explicitly [35, 36].

2.1.2. Pathway Models

The response of coasts to storms and the extent of flooding can be assessed with computational models, which numerically solve the physical equations that govern the motion of water and sediment in the nearshore and the hinterland. A number of different models [e.g., 15, 16, 17, 18], varying in their numerical solutions, spatial dimensions and the range of physical processes included, have been successfully applied to the problem of hazard modeling in different coastal settings [e.g., 37, 38, 39]. The models are driven by time series of meteorological or hydraulic variables at the offshore boundary of their domain. Their output contains time series of hydraulic or morphological variables, which are potential hazards at the shore and in the hinterland, on a structured or unstructured numerical grid.

2.1.3. Consequence Models for Receptors

Diverse and complex consequences can arise from flooding or erosion. Separate approaches can estimate economic, political, social, cultural, environmental or health-related consequences. In general, these approaches operate on the receptor level. Most commonly, they are functions, often referred to as vulnerability relationships, which map one or multiple hazards to consequences for a specific type of receptor. Literature reviews on vulnerability relationships exist, for instance, for economic damage [21], health impacts [19, 20], and the loss of life [40] due to flooding.

2.2. Disaster Risk Reduction Measures in Models

According to the terminology of the United Nations Office for Disaster Risk Reduction, DRR measures reduce the exposure to hazards or lessen the vulnerability of receptors [21]. For modeling, a similar categorization into three types is useful, as we explain below. Exposure-reducing measures move receptors out of high risk areas, for instance, by temporally evacuating people or permanently relocating residential areas. Pathway-obstructing measures change the bathymetry and hence its interactions with waves and water levels. Examples are beach or dune nourishment, revetments and floodwalls. The third type are
vulnerability reducing measures, which include for instance flood protection for individual receptors. Also raising the awareness of potential flooding and flood impacts amongst inhabitants belongs to this category.

Modeling the effect of DRR measures belonging to one of the first two types is straightforward. For exposure-reducing measures, receptors are excluded from the model or different types of land-use can be assumed for high risk areas. For pathway-obstructing measures, the pathway models can be modified and the effect simulated. Modeling vulnerability-reducing measures is more intricate. In principle, their effect is assessed by modifying consequence models [e.g., 42]. Some such measures such as early warning or awareness raising, depend on effective uptake or operation by people. To accommodate this, Cumiskey et al. [43] developed a methodology to quantify and aggregate factors that influence uptake and operation.

2.3. Bayesian Networks

In this section we explain the basic theory of BNs, as we will use them to integrate the individual approaches into a homogeneous framework. BNs represent a joint probability distribution over a set of random variables. If one or more variables are observed, the BN evaluates the influence of this new evidence on the distributions of all other variables. If the model is “small enough”, it can predict changes in distributions instantly and can be interpreted intuitively. For this reason, BNs have been used as early warning systems for natural hazards [23, 44, 45] and as input for negotiations and discussions between experts, managers, stakeholders and citizens [46, 47, 48]. In coastal settings, such models have been shown to successfully predict erosion and shoreline retreat [49, 50, 51]. BNs have also proved to be valuable for estimating damages to residential buildings after hurricanes [52] and to evaluate the risk to nuclear facilities from coastal hazards [53].

A discrete BN represents the joint probability mass function of a set of random variables \(X = \{X_1, \ldots, X_n\}\) as a directed acyclic graph [54, 55]. Each variable constitutes a node in the graph. The nodes are connected by arcs which indicate potential dependence between variables. The direction of an arc, from so-called parent to child, signifies the direction of influence. The arcs must not form a cycle; no path \(X_i \rightarrow \cdots \rightarrow X_i\) may exist for any \(i = 1, \ldots, n\). Figure 2 illustrates such a graph structure.

The semantics of the graph stipulate that each \(X_i\) is conditionally independent of all predecessors given its parents. Therefore, a joint probability distribution \(P(X_1, \ldots, X_n)\) can be economically factorized through the chain rule:

\[
P(X_1, \ldots, X_n) = \prod_{i=1}^{n} P(X_i | pa(X_i)), \tag{1}
\]

\(^1\)We do not consider continuous BNs in this article.
where $pa(X_i)$ denotes the set of parent nodes of $X_i$. The factors $P(X_i \mid pa(X_i))$ on the right hand side of the equation are stored as conditional probability tables (CPTs), or in case of no parents as probability tables (PTs), and associated with each node $X_i$. Together, the graph semantics and all CPTs uniquely specify the joint probability mass function of $X$.

A BN’s computing algorithm uses Bayes’ theorem. Lauritzen and Spiegelhalter [56] developed exact algorithms for high dimensions, which are implemented in most BN software. In two dimensions the theorem is given by

$$P(X_1 \mid X_2) = \frac{P(X_2 \mid X_1)P(X_1)}{P(X_2)}.$$ (2)

$P(X_2 \mid X_1)$ is the CPT of node $X_2$. $P(X_1|X_2)$, which is computed, is called the posterior distribution, and can be interpreted as the updated distribution of $X_1$ taking into account new evidence on $X_2$.

The CPTs and PTs can be learned from data, specified based on experts’ estimates or derived from equations. In the next section, we describe the general structure of the DSS and explain how we quantified the CPTs and PTs.

3. Design of the Decision Support System

3.1. Overview

The BN that we designed as a DSS for coastal risk management has five categories of variables: Boundary condition (BC), receptor type (R), hazard (H), consequence (C), and DRR measure (M). Figure 3 shows a high-level framework of the DSS and illustrates the influences from variables of one category onto another. If in an application each category had only one variable, then this representation would correspond to the BN graph. There are no arcs between variables of the same category. As a consequence, all boundary conditions, receptor types and DRR measures are mutually independent, while hazards and consequences are conditionally independent of each other given their parents.

Admittedly, this assumption may appear unnatural for boundary conditions and DRR measures. We reflect on this issue when describing those categories in Sections 3.3 and 3.4.1.
All boundary conditions influence all hazards, which is indicated by the solid arc in Figure 3. In contrast, each type of receptor (e.g., people, buildings, infrastructure, and ecosystems) has a sub-module in the BN. It consists of an $R$ node (representing the locations of receptors on the site) as well as $H$ nodes (representing the hazards given the receptors’ locations) and $C$ nodes (representing the consequences given (some of) the receptors’ hazards). The dashed arcs in Figure 3 represent the fact that the sub-modules are not directly interconnected. Nevertheless, dependencies arise from the common parents, which are boundary conditions and, possibly, DRR measures.

While the high-level representation is generic, the BN is tailored to case study sites through the choice of variables and the supplied training data, based on the characteristics of the site under investigation. Owing to the generic structure, the process of constructing the BN can be automated and, if desired, integrated with open shell systems that manage forecasting processes, such as Delft-FEWS [57]. We developed specific file formats in which variable definitions and training data need to be provided, as well as a C++ program to read them and create a BN. The source code is open and available at https://github.com/openearth/coastal-dss. An executable for Windows and documentation is also provided. The core of our program builds on SMILE, which is a reasoning engine for graphical models. It is available free of charge for academic research and teaching use from BayesFusion, LLC, http://www.bayesfusion.com/.

3.2. Training Data

In essence, the training data comprises a set of storm simulations, cadastral information on the case study site, and vulnerability relationships (cf. section 2.1.3). Additional data may be required to include risk reduction measures, as described in Section 3.3.

The set of simulations should reflect the storm climate of the site. Each storm is defined by an offshore time series of waves and water levels, which is typically assumed to be uniform along the offshore boundary, and the simulation shows its propagation into the hinterland. For simplicity, we use statistics of the offshore
time series, such as maxima and averages, to characterize the storm. In our decision support framework, these statistics are the variables of the BC category. Ideally, the storm scenarios are derived from a multivariate statistical analysis of measured wave and water level time series [e.g., 23, 35] and can be a combination of historical and synthetic events. However, if adequate data or analysis tools are not available, the scenarios can also be derived from expert opinion (e.g., with the classical model for structured expert judgment and extensions thereof [58, 59].

As the BC category is related to input of the simulations, the H category is related to output. Statistics of the gridded time series of hydraulic or morphological variables in the hinterland constitute the H variables. Finally, the data for the R variables stem from the cadastral information and the data for the C variables are estimated from the H variables using vulnerability relationships. In each category, the CPTs or PTs of the variables are learned differently, as will be explained in the following section.

3.3. Including DRR Measures

DRR measures do not have PTs. They are implemented as decision nodes and not as random nodes, because their states represent the actions of decision makers. For the same reason, measures are not interconnected with arcs. To avoid situations in which incompatible measures are simultaneously selected, they can be treated as different states of the same variable. When there are no conflicts, the variables typically have two states (“in place” and “not in place”).

The three types of measures described in Section 2.2 can be incorporated into the BN. To demonstrate the outcome from exposure-reducing measures, we conceptually move receptors to a safe zone. To show the effect the pathway obstructing measures, we simulate different storm scenarios with the original and the adapted bathymetry. Finally, we modify vulnerability relationships and, if applicable, include a measure effectiveness factor to account for effective uptake and operation of vulnerability-reducing measures.

3.4. Quantification of (Conditional) Probability Tables

3.4.1. Boundary Conditions

The BN learns the PTs of BC nodes from storm simulations. The PT entries are set to the relative frequencies of observed values in all simulations. Although there may be notable dependencies between hydraulic boundary conditions (cf. Section 2.1.1), these are not modeled with the current version of the program; boundary conditions do not have parents. We reflect on the implications of this assumption in the discussion (Section 5).

\[\text{While we include decision nodes, our model is not an influence diagram, because it does not solve for an optimal decision in terms of a maximum expected utility.}\]
3.4.2. Receptors

Each receptor type, such as building, people or infrastructure, is associated with a node that characterizes the location of a randomly selected object or individual. To this end, the case study site is divided into zones (including the external safe area, if applicable). A division is subjective and depends on features of the site; natural topological or political boundaries can be used. The zones are identical for all receptor types.

Figure 4 shows an illustration site with 26 houses across two zones: the beachfront and inland. We denote the node for the receptor type house as $X_{\text{house}}$. To understand why we consider the location of an individual house as uncertain, imagine selecting one of them randomly, just like drawing a ball from an urn. The probability for a house to be within a given zone is proportional to the total number of houses in that zone. Because 10 houses are located at the beachfront and 16 inland at the illustration site, $P(X_{\text{house}} = \text{beachfront}) = \frac{5}{13}$ and $P(X_{\text{house}} = \text{inland}) = \frac{8}{13}$. The same entries of the PT can be thought of as a spatial distribution of the houses in terms of the zones.

Note that the number of receptors in a zone could change for different combinations of exposure influencing DRR measures. In that case $X_{\text{house}}$ would have a CPT and not a PT, because DRR measure variables would be parent nodes.

![Figure 4](image)

Figure 4: Illustration site with 26 houses distributed across 2 zones. The color of a house indicates its degree of flooding: none is white, medium is white-blue, and high is blue.

3.4.3. Hazards

The BN learns the CPTs of hazards from storm simulations as well, however in a different manner than the PTs of boundary conditions. Now, the CPT entries represent, for each degree of hazard severity, an estimate for the proportion of affected objects or individuals. They can also be interpreted as the probability of degree of hazard severity for a randomly selected receptor. Of course the proportions vary depending on the zone, the boundary conditions and the DRR measures in place.

We illustrate the learning with an example and refer the reader to Appendix A for the precise algorithm. Consider again the illustration in Figure 4. We call the combination of boundary conditions and DRR measures a scenario. The hazard variable, flood depth, has three states: none, medium and high. The flood depth at each house is indicated by its color: white, white-blue or
blue. In the beachfront zone, \(\frac{3}{10}\) houses experience a high flood depth, \(\frac{6}{10}\) a medium depth, and \(\frac{1}{10}\) none. These three numbers are the CPT entries given the scenario and for the zone beachfront. Similarly, the entries are \(\frac{3}{16}\), \(\frac{6}{16}\) and \(\frac{7}{16}\), for the zone inland under the same scenario.

Because the local features of a site influence the flood flow, the degree to which a receptor is affected depends on its exact location. Without resolving to the spatial scale of individual receptors, this is reflected by the above fractions. As other types of receptors have a different spatial configuration (and total number), their fractions are different. Therefore, we model hazards separately for each receptor type.

Finally, due to the discretization, it is not possible to distinguish storms whose boundary conditions fall into the same pre-defined states. In such cases, we average the observed fractions.

### 3.4.4. Consequences

Consequences have truth tables, which are a special case of CPT. In a truth table each combination of parent states corresponds to a single child state with probability 1. Hence, the relationship of consequences to their parents is deterministic. In this BN, we use vulnerability relationships, which are commonly used in the field (cf. section 2.1.3), to compute consequences as a function of hazards and DRR measures.

### 4. Application to North Norfolk, UK

#### 4.1. Case Study Site

The North Norfolk coast is a north-facing coastline, characterized by both gravel and sand barriers, with an extensive (>2000ha) saltmarsh area behind barrier islands, spits and areas of low gradient sand flats on open coasts. In this area the natural environment is a major source of revenue for the local economy via its contribution to nature-based tourism and recreational uses. Analysis of coastal hazards along this stretch of coast has highlighted Wells-next-the-Sea as a risk hot spot [60].

Wells is a small coastal town (population 2165, 2011 Census). It is the largest urban center on the North Norfolk coast. The main industry of Wells is tourism, but there is also a small fishing and a wind farm servicing industry. The town has a long history of flooding due to storm surges. As such, the coastal defenses have been improved over time. The embankment forming the western side of the Wells Harbour Channel breached in the catastrophic storm of 1953 [61] and again in the storm surge of 1978 [62], leading to considerable areas being flooded on the western side of the town. Following the storm surge of 1978, this embankment was re-built to a much higher specification and, as a consequence, withstood the December 2013 surge with minimal damage [63]. In addition, the raising of the flood wall to the south of this embankment and the construction of a movable barrier between this defense and the building line at the back of the Wells Quay has reduced the risk of flooding to the low-lying
western part of the town. Some individual residential and commercial properties have also implemented property level protection measures.

4.2. BN Specification

Following the general structure introduced in Figure 3, the BN for Wells has boundary conditions, DRR measures, receptors, hazards and consequences. Figure 5 shows the graph of the BN. The boundary conditions are maximum water level and maximum wave height. There are four receptor types, each with its own hazards and consequences. For residential and commercial properties we include flood depth and absolute monetary damage. For people we assess the maximum depth-velocity product experienced and the risk to life. For the saltmarsh, we include flood depths and wave height, and damage in terms of an ecosystem vulnerability indicator (cf. Table 2). Finally, there are two pathway obstructing measures (extending the sea wall and increasing its height) and a vulnerability reducing measure (raising awareness through display boards).

The BN is trained with 85 storm scenarios representing the range of potential extreme event conditions, which are generated from coastal scale modeling. They include historical storms (8 scenarios), climate change (18 scenarios) and synthetic events (59 scenarios).

4.2.1. Boundary Conditions

We defined the extreme events at Wells in terms of the peak water level and maximum significant wave height. We calculated the boundary conditions from a model train (Figure 6), which transforms coarse external model conditions to detailed model results at the BN boundary condition location (Wells harbour channel entrance, 52.993N 0.853E) and generates the input conditions for the model train to calculate the subsequent flooding.

The model train uses predicted hindcast data at 12 locations from the CS3 (before 2007) and CS3X (post 2007) tidal surge model run by the National Oceanography Centre, UK (NOC). The model predicts hourly tide and surge residual data with a resolution of approximately 12km which are used to drive a 2D TELEMAC model [16]. The TELEMAC model extends 50km offshore from the case study site, over an area of 4750 km$^2$. The unstructured grid consists of 10,704 elements with 5759 nodes. The largest elements have a resolution of 12km but the grid resolution becomes finer towards the coast with the smallest resolutions in the Wells Harbour channel of approximately 15m.

The wave conditions are generated at the entrance to the harbour channel by 2 nested SWAN models [64]. The nested SWAN models are driven by 2D spectra from the UK Met Office Wavewatch III (WWIII) North Atlantic European model with a resolution of approximately 12km. The Met Office model has a spectral resolution of 25 frequency bins and 24 directional bins. It is forced by a 10m wind field from the Met Office Numerical Weather Prediction models and the Global Wave Model. The wind characteristics are obtained from the 10m wind field from the Met Office Numerical Weather Prediction model. The water level and flow velocities are obtained from the TELEMAC model and
interpolated onto the nested SWAN model grids. The largest of those grids
covers an area of 90 x 60km with a resolution of 5km, the smaller grid covers an area of 32 x 13km with a resolution of 500m. Wave growth from wind, whitecapping, quadruplets, breaking waves, diffraction, triad interactions and setup are included in the models using the present default settings (SWAN version 41.01 [55]).

The historic storm events were generated by external model hindcast storms selected where boundary conditions were available from external models. In total eight historic storm surge events were selected: 20-21 February 1993, 10 January 1995, 19-20 January 1996, 14 December 2003, 31 October-3 November 2006, 17-20 March 2007, 7-10 November 2007, and 4-7 December 2013. Synthetic storm events were generated to produce a fuller range of potential storms based on historic surge and wave conditions. The synthetic storms were generated using a typical spring tide, with length of 55 hours, with the addition of a storm surge residual from one of eight historic storm surges. The peak storm surge residual coincided with the peak tidal water level. To create a greater range of synthetic storms the spring tide or storm surge residuals were multiplied by a factor (0.7 - 1.3). Analysis of the historic surge events found no clear dependencies between the surge and wave characteristics. At this location it is clear that it is the high water levels, usually caused by the coincidence of a surge event with high water on a high spring tide, which generates the flooding. In order to create representative wave conditions which are likely to occur with a surge, the synthetic storm wave and wind conditions were taken from the historic storm events. The synthetic storms cover a range of conditions up to a return period of 400 years, based on peak water level. Only those synthetic storms which had an impact are included in the BN.

Climate change scenarios were generated by modifying the boundary conditions from the historical storm event hindcast model to include a sea level rise prediction. The climate change scenario sea level and surge data were based on the IPCC (2013) RCP8.5 (Representative Concentration Pathway) projections for 2060. The future extreme storm surge levels (SSL) along the European coasts have been predicted by Vousdoukas et al. [66], using a DELFT3D-Flow model forced by an 8 member climate model ensemble. The authors predict the RCP8.5 2060 relative sea level rise (RSLR) at the case study site (52.98N 1.228E) to be +39cm and the predicted change in surge height in 2060 for a 20 year return period is -4cm, giving an overall climate effect of +35cm.

4.2.2. Receptors

We divided the case study site into 6 zones, based on topographic features and key current flood prevention measures, such as the flood wall and movable flood barrier. The receptor types are residential property, commercial property, people and saltmarsh. Their locations are shown in Figure [7]. We did not include caravans as receptors themselves, but we did include the people living inside the caravans in the analysis. We considered people to be inside their homes/caravans at the time of the flooding impact. The model assumed a ratio of 3:1 for the number of people in houses to caravans.
4.2.3. Hazards

We obtained detailed hazard values (inundation depth, flow velocity, wave height) by modeling the flood inundation in the study area and by mapping the receptor locations at their nearest grid point.

A small SWAN model (4 x 4km with a resolution of 15m) calculates the wave height within the harbor channel. It includes the wave energy dissipation due to the saltmarsh vegetation adjacent to the Wells Harbor (plant height=0.11m, field data from Stiffkey, North Norfolk [67]; plant diameter=0.00125m [68], plant density=1061 plants per m$^2$, field data at Tillingham, Essex [69]). From the SWAN model we obtained water level and wave conditions at 64 locations along the Wells Harbor Channel. We calculated overtopping rates at transects at these 64 locations using EurOtop [70] and used the resulting overtopping discharge to drive a flood inundation model for the town. The inundation model covers an area of 7.5km$^2$, the whole of Wells-next-the-Sea and some of the surrounding countryside. The landward margin of the flood grid is defined by the 10m Ordnance Datum Newlyn (ODN) contour. The majority of the grid has an approximately 12.5m resolution. A finer resolution is needed to represent the current flood wall and DRR measures in the mesh; therefore a resolution of 0.5m is used at the wall.

4.2.4. Consequences

We determined the impact of the flooding with vulnerability relationships. For residential properties, we estimated the potential absolute damage from the

Figure 7: Defined zones in Wells-next-the-Sea and receptor locations
inundation depth. To do that, we applied UK depth-damage curves for semi-detached houses [71], the most common property type in Wells. The residential properties are divided into those with flood protection and those without protection. From a site and Google Street View survey only 17 of 960 houses below 10m ODN were found to have any form of property level protection measures in place. We assumed that if flood resistance measures are present the house had up to date protection to the current standards. UK industry standards assume that resistance measures protect up to 0.6m above the threshold of the house [71]. The depth-damage curves were therefore modified for properties with flood protection, so that no damage occurred below 0.6m.

Commercial properties are also divided into those that have flood resistance measures and those that are unprotected (surveys found 10 properties with flood protection out of a total of 140 surveyed). Commercial properties within the case study site are typically small shops, restaurants, pubs, cafés and small warehouses. We assumed that the depth-damage curve data for retail adequately represents the commercial properties in the case study site. We obtained the depth-damage curve data from Penning-Rowsell et al. [71] for retail properties with no cellar, a short duration flood and a mean area of 140.45m². We modified the curve following the same principle as for the residential properties with flood resistance measures.

As is common in the field, we calculated risk to life through the matrix developed by Priest et al. [72], which is based on the depth velocity product experienced and the vulnerability of the area (Table 1). Vulnerability of the area is based on the type of buildings and the construction methods at three levels: low vulnerability is applied to masonry, concrete and brick buildings; medium vulnerability is applied to mixed building types and high vulnerability is applied to caravans, campsites, bungalows and poorly constructed buildings. We assumed that the area is largely medium vulnerability, as it is a typical residential area with mixed type of properties. An exception is zone 1 to the west of the earthen embankment at the edge of the Wells Channel, which we defined as a high vulnerability area due to the large number of caravans (568 caravans in zone 1).

<table>
<thead>
<tr>
<th>Depth Velocity product m² s⁻¹</th>
<th>Low Vulnerability</th>
<th>Medium Vulnerability</th>
<th>High vulnerability</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;0.25</td>
<td>Low risk</td>
<td>Low risk</td>
<td>Low risk</td>
</tr>
<tr>
<td>0.25-0.50</td>
<td>Low risk</td>
<td>Medium risk</td>
<td>Medium risk</td>
</tr>
<tr>
<td>0.50-1.10</td>
<td>Medium risk</td>
<td>Medium risk</td>
<td>High risk</td>
</tr>
<tr>
<td>1.10-7</td>
<td>Medium risk</td>
<td>High risk</td>
<td>Extreme risk</td>
</tr>
<tr>
<td>&gt;7</td>
<td>Extreme risk</td>
<td>Extreme risk</td>
<td>Extreme risk</td>
</tr>
</tbody>
</table>

Table 1: Risk to Life matrix [72], relating the depth-velocity product experienced during a flood event and the area vulnerability to the risk to life.

We estimated the damage to the saltmarsh by a ecosystem vulnerability indicator (Table 2), which relates damage to inundation depth and maximum wave height. We developed the saltmarsh vulnerability indicator from the work of Woodroffe [73] and Möller et al. [68]. We assumed the saltmarsh at the case...
The study site is an open coast marsh in a mesotidal area. For inclusion in the BN, the saltmarsh was divided into 372 individual units, based on the grid node locations of the TELEMAC model.

<table>
<thead>
<tr>
<th>Depth (m)</th>
<th>Wave Height (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>&lt;0.3</td>
</tr>
<tr>
<td>0 to 1</td>
<td>0</td>
</tr>
<tr>
<td>1 to 2</td>
<td>0</td>
</tr>
<tr>
<td>2 to 3</td>
<td>0</td>
</tr>
<tr>
<td>3 to 4</td>
<td>0</td>
</tr>
</tbody>
</table>

0: No effect  
1: Changes within normal seasonal variation  
2: Changes beyond normal seasonal variation, but partial/total recovery  
3: Irreversible change  

Table 2: Saltmarsh Ecosystem Vulnerability Indicator [74]  

4.2.5. DRR Measures

We tested two structural DRR measures: i) an extended flood wall and ii) increasing the height of the flood wall in combination with a movable barrier. We ran modified versions of the TELEMAC flood model to assess the change in the hazard experienced by the receptors. The extended flood wall lengthens the existing wall along the front of the harbor quay, protecting the properties in Area 3. The higher flood wall was chosen as water levels for the recent 2013 storm surge event almost reached the top of the existing defenses.

Additionally, we included iii) a vulnerability influencing DRR measure in the BN. This takes the form of a series of display boards containing cartographic information on former shoreline positions to demonstrate coastal dynamics, and images of flood markers along the coast to indicate elevations reached by historic storm surges. The aim of the display boards is to increase awareness of flood risk, with a hoped-for increase in property level protection.

To determine the effectiveness of the display boards we employed the method of Cumiskey et al. [43], which assumes that the effectiveness of DRR measure depends on three factors: uptake, operator and performance. The values for each of these factors are displayed in Table 3. Uptake is the percentage of the population who will adopt the measure. We calculated a value of 9% based on 50% of the population will see the display board, 30% of the population will want to take action as the threat and coping appraisal level are high and 60% of the population can afford the measures due to an above average income level. The operator factor is the percentage of the population that will operate the measure before a flood, calculated as 77.3%. The Environment Agency [75] gives an operator value of 86.1%, which was adjusted down as 24% of the population within the North Norfolk Area of Natural Beauty (AONB) are second home owners. We assumed that a third of the second homes would have someone available to operate the flood protection (due to the probability of an event occurring at a weekend or holiday when second home owners are more likely to be in residence) (72.3% operator value). With the use of the display boards it is expected that more of the population will be reminded to check they know how to operate the measures they have, giving a post DRR operation measure of 77.3%. The performance factor is the percentage of the population who...
will operate the measure effectively. We calculated a value of 73% from the assumptions that 5% of equipment are lost or misplaced, 95% of the product are in good working order, 90% of the population receive a flood warning, and that there is a 90% chance that flood heights do not exceed flood protection level [76].

By combining the factors, we estimate an increase of property level protection with the display board DRR of 5.08%. While it is possible to include the increase in protection as a measure effectiveness node, in this instance, we have directly modified the vulnerability relationships accordingly.

<table>
<thead>
<tr>
<th>Influencing Factors</th>
<th>Post DRR measure</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Uptake</strong>: % of the population who will adopt the measure</td>
<td>9%</td>
</tr>
<tr>
<td><strong>Operator</strong>: % of the population that will operate the measure before a flood</td>
<td>77.3%</td>
</tr>
<tr>
<td><strong>Performance</strong>: % of the population who will operate the measure effectively</td>
<td>73%</td>
</tr>
</tbody>
</table>

Table 3: Influencing factors for the effectiveness of the display board DRR measure

4.3. Results

We could predict hazards and impacts in Wells with the BN in real-time without the need for further detailed flood modeling, as the BN is trained with a range of potential storms. The BN also allowed the impact and cost-effectiveness of the DRR measures to be studied. The quantified model with its prior probabilities can be seen in Figure B.10 in Appendix B. In this section, we describe the BN results for a storm of 4.41 m water level and 2.17 m significant wave height. This storm was calculated as the 1 in 100 year return period storm based on the maximum water level only. For reference, the BN constraint on these bins is given in Figure B.11 in Appendix B.

The majority, 93.55%, of residential properties had no flood inundation and therefore sustained no damages (Figure 8a). Maximum inundation depths with an associated absolute damage of £30,000-55,000 reached 0.49% of the properties. The higher sea wall had little effect on the absolute damage distribution (Figure 8c). The extended sea wall shifted the distribution of damage to lower values (Figure 8b). Display boards can be applied together with any of the structural measure options. Whilst the display boards had little influence on the largest damage bins, due to the property level protection only protecting up to 0.6m, the distribution of damage shifted to lower levels below 0.6m (Figure 8d, 8e, 8f).

Commercial properties were at a greater risk in this scenario with 36.6% of commercial properties experiencing some flooding with no DRR measures in place (Figure 9a). 5.91% of commercial properties were inundated by 1-3m resulting in absolute damage of £120,000 to 200,000. Again, the higher sea wall, showed little damage reduction, suggesting that this is not a suitable measure for this storm scenario (Figure 9c). The extended sea wall reduced the number of commercial properties experiencing the highest levels of absolute damage (Figure 9b). The Display Board showed a shift to lower levels of damage for
all the scenarios tested. However, they had no influence on the higher damage levels due to the flood protection height limit (Figure 9d, 9e, 9f).

Figure 8: Absolute Residential Damage values for the 1 in 100 year return period storm with a) No DRR measures, b) Extended sea wall c) Higher sea wall d) Display Boards e) Display Boards and Extended sea wall and f) Display Boards and Higher sea wall

Figure 9: Absolute Commercial Damage values for the 1 in 100 year return period storm with a) No DRR measures, b) Extended sea wall c) Higher sea wall d) Display Boards e) Display Boards and Extended sea wall and f) Display Boards and Higher sea wall
97.6% of the people were not at risk to life, 2.3% at a low risk and 0.1% at a medium risk. The risk to life changed through the hazard influencing DRR measures, as the measures modified the maximum depth-velocity product in Wells. With an extended sea wall, risk to life was reduced compared to the no DRR case. 98.3% of the population was at no risk and 1.6% at a low risk. The higher sea wall had negligible influence on the risk to life. 97.5% of the population was at no risk, 2.3% at low and 0.1% at medium risk.

The saltmarsh was not influenced by the DRR measures due to its location seaward. For this 1 in 100 year storm, 98.3% of saltmarsh was undamaged, while 1.54% of the saltmarsh experienced changes within the normal seasonal variation of saltmarsh condition.

We observed similar effects of the DRR measures across all the storm scenarios of the BN. The higher sea wall showed a very similar distribution of damage to the no DRR measure option for all the storm scenarios, suggesting that the higher sea wall is not a suitable DRR measure at this location. The extended sea wall led to a slight reduction in damage to residential properties, a slight reduction in risk to life and a larger reduction in damage to commercial property. The display board DRR measure showed a general reduction in commercial and property damage for those properties with low inundation depth, however, at large flood depths this DRR measure had no effect.

5. Discussion

In this section we reflect on a number of aspects related to limitations and potential of the approach. A main advantage of the BN framework is that we can immediately predict what proportions of receptors experience hazards and consequences in distinct spatial zones of a site, when we impose evidence for the offshore boundary conditions of a storm scenario. This property is useful in operational forecasting and early warning systems. Many of them rely on ensemble forecasting to account for (some of the) uncertainties in initial conditions and model formulations of numerical weather predictions and regional hydrodynamics and wave models (e.g., see references in [77]). Hence, the boundary conditions that the BN should evaluate in the hot phase could be an ensemble instead of a point forecast. The BN could deal with such forecasts.

To explain how, we first consider the simple case of a single boundary condition variable influencing a single hazard variable. We recall that given a regular point estimate for the boundary condition, the BN predicts a distribution for the hazard. In the present application, the distribution can be interpreted as the proportions of receptors in the area that are affected. Thus, an ensemble of boundary conditions would link to an ensemble of hazard distributions. In the BN, we can set the distribution of the boundary condition node so that it represents the ensemble members. The updated hazard distribution would then

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3For technical details on integrating the BN into forecasting systems see Bogaard et al. [57]. They describe the integration into Delft-FEWS, a generic tool to set up such systems.
be an estimate of the ensemble mean hazard distribution. Additionally, we can obtain a worst-case and best-case hazard distribution, by conditioning on the lightest and the most severe boundary conditions, respectively.

In principle, the ensemble mean can be estimated for multiple boundary conditions as well, but we might introduce error, because they are modeled as independent in the BN. This model assumption is generally unproblematic for predictions based on fixed values of all boundary conditions. However, neglecting those dependencies can limit the BN’s applicability for other purposes. In particular, this simplification can introduce error to the estimates of unconditional hazard and consequence probabilities, as the BN evaluates the law of total probability. These probabilities would be necessary for risk assessments and to find the most economical suite of DRR measures [e.g., 78, 79]. The situation is similar for hazard and consequence probabilities that are computed for updated distributions of boundary conditions, for instance to represent an ensemble forecast. Finally, the assumption could also have effects on the diagnostic reasoning (i.e., in opposite arc direction) of the BN, because then the unconditional hazard and impact probabilities appear in the denominator of Bayes’ theorem.

To expand the BN’s potential for wider applications, the graph structure dictated by the framework should be adapted so that it can represent the multivariate distribution of boundary conditions at case study sites more realistically. We also recommend, to investigate the influence of different discretizations on the dependence structure and, if necessary, to optimize it per site. Of course, a prerequisite for these extensions would be a multivariate statistical analysis of available boundary condition measurements or hindcast for the location of interest, for instance with copula-based approaches [13, 14].

Finally, a general limitation of the proposed BN approach is its reliance on synthetic data. While we need modeled data to gain insight into hazards and impacts of storms when field observations are lacking, the validity of the BN depends on the validity of the underlying data-generating models. At present, we do not account for imperfections in those models, but future research should explore the sensitivity of BN predictions to errors or uncertainties in the data generation process.

6. Conclusion

We developed a BN approach to support decision making in coastal risk management. An important contribution is the learning algorithm for the BN, which integrates output from storm simulations with land use data, vulnerability relationships and DRR measures. The algorithm is programmed in C++ and openly available at https://github.com/openearth/coastal-dss. We described the application to a small town in North Norfolk, UK, which is a risk hot spot during coastal storms.

The case study demonstrates how information flows through the BN and how it can predict onshore hazards and impacts, when provided with evidence of the offshore boundary conditions of a storm scenario. Because detailed data of severe storms including their hazards and impacts are almost never available,
the BN learns from a database of hindcast and synthetic events. Each event in the database is simulated with a 2D physics-based numerical model that covers the hot spot area. This way, the training data set captures the dependence between boundary conditions and various hazards, such as erosion and flood velocity, and reflects the complex influence of the local bathymetry. At this stage, we take the precise locations of receptors into account. We include the dependence between hazards and impacts via vulnerability relationships, such as depth-damage-curves. Finally, we can also incorporate DRR measures. If they are structural, they are added through additional simulations with altered bathymetry. Otherwise, we assign them modified spatial distributions of receptors or vulnerability relationships.

The resulting BN forms a comprehensive and concise representation of risk propagation in a complex system of physical, ecological and human components. From a practical point of view, this integrative character, together with the capability to predict in real-time, makes the BN a helpful tool for decision makers. From a scientific point of view, the model development approach emphasizes how results from multiple disciplines must be connected in order to understand risks and can provide an objective basis for choosing DRR measures.

7. Acknowledgments

This work was supported by the European Community’s 7th Framework Programme through the grant to RISC-KIT (“Resilience-increasing Strategies for Coasts - Toolkit”), contract no. 603458, and by contributions by the partner institutes. The authors would like to thank Nathaniel Plant for the fruitful discussions on this research. We would also like to thank the two anonymous reviewers for their valuable comments which helped to improve this manuscript.

References


Appendix A. Learning Algorithm for the Conditional Probability Tables of Hazard Nodes

Let $X_{hr}$ denote a hazard node for receptor type $r$ with states $s_{hr} = 1, \ldots, S_{hr}$. We denote DRR measures, boundary conditions and receptors analogously using the subscripts $m$, $bc$ and $r$ (cf. Table A.4).

Before learning the CPT, we introduce an experience matrix, $E$, of size $S_{bc} \times S_{m\in pa(h_r)}$. $S_{bc}$ is the vector of number of states of all boundary conditions.
Table A.4: Nomenclature for CPT learning

<table>
<thead>
<tr>
<th>Super- or Subscripts</th>
<th>Variables</th>
<th>Constants</th>
</tr>
</thead>
<tbody>
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<td>( n )</td>
<td>( X_{bc} )</td>
<td>( S_{bc} )</td>
</tr>
<tr>
<td></td>
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<tr>
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<td>( E )</td>
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</tr>
<tr>
<td>( h )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( pa )</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

- **Super- or Subscripts**
  - \( n \): simulation index
  - \( bc \): boundary condition index
  - \( m \): DRR measure index
  - \( r \): receptor type index
  - \( h \): hazard index
  - \( pa \): parent set

- **Variables**
  - \( X_{bc} \): boundary condition \( bc \)
  - \( X_{m} \): DRR measure \( m \)
  - \( X_{r} \): receptor type \( r \)
  - \( X_{hr} \): hazard \( h \) for receptor type \( r \)
  - \( E \): experience matrix

- **Constants**
  - \( S_{bc} \): number of states of \( X_{bc} \)
  - \( S_{m} \): number of states of \( X_{m} \)
  - \( S_{r} \): number of states of \( X_{r} \)
  - \( S_{hr} \): number of states of \( X_{hr} \)

\[ E^{(n)}[s_{bc}^{(n)}, s_{m \in pa(h_r)}^{(n)}] = E^{(n-1)}[s_{bc}^{(n)}, s_{m \in pa(h_r)}^{(n)}] + 1. \quad (A.1) \]

Here, \( s_{bc}^{(n)} \) and \( s_{m \in pa(h_r)}^{(n)} \) denote the states of \( X_{bc}^{(n)} \) and \( X_{m \in pa(h_r)}^{(n)} \) in simulation \( n \). Then, we compute, for each \( s_{r} \) and \( s_{hr} \),

\[
P_{r}^{(n)}(X_{hr} = s_{hr} \mid X_{bc} = s_{bc}^{(n)}, X_{m \in pa(h_r)} = s_{m \in pa(h_r)}^{(n)}, X_{r} = s_{r})
= \frac{m_{s_{hr} \rightarrow s_{hr}}^{(n)} - p_{X_{hr} \mid X_{bc} = s_{bc}^{(n)}, X_{m \in pa(h_r)} = s_{m \in pa(h_r)}^{(n)}, X_{r} = s_{r}}^{(n-1)} \cdot E^{(n-1)}[s_{bc}^{(n)}, s_{m \in pa(h_r)}^{(n)}]}{E^{(n)}[s_{bc}^{(n)}, s_{m \in pa(h_r)}^{(n)}]}, \quad (A.2)\]

where \( m_{s_{hr} \rightarrow s_{hr}}^{(n)} \) is the number of receptors of type \( r \) in zone \( s_{r} \) that experience hazard \( X_{hr} \) in state \( s_{hr} \) in simulation \( n \). Further, we used \( p_{X_{hr} \mid X_{bc} = s_{bc}^{(n)}, X_{m \in pa(h_r)} = s_{m \in pa(h_r)}^{(n)}, X_{r} = s_{r}}^{(n-1)} \) to denote \( P_{r}^{(n-1)}(X_{hr} = s_{hr} \mid X_{bc} = s_{bc}^{(n)}, X_{m \in pa(h_r)} = s_{m \in pa(h_r)}^{(n)}, X_{r} = s_{r}) \).

Thus, according to equation \( A.2 \), the CPT entries represent average proportions of receptors of type \( r \) subjected to \( s_{hr} \) over all simulations with identical states for boundary conditions and DRR measures.
Appendix B. BN for Wells-next-the-Sea in GeNIe

As graphical user interface for the BNs we used GeNIe, which is available free of charge for academic research and teaching use from BayesFusion, LLC, http://www.bayesfusion.com/. Because the state names of the nodes in GeNIe must be strings with no spaces and no symbols, we resorted to special characters to represent positive or negative values, decimals and ranges (Table B.5).

Figure B.10 shows the quantified BNs with its prior distributions and Figure B.11 shows the quantified BN conditioned on the states corresponding to a 1 in 100 year return storm (water level = 4.41m; wave height = 2.17m).

<table>
<thead>
<tr>
<th>Special character</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>p</td>
<td>+</td>
</tr>
<tr>
<td>m</td>
<td>−</td>
</tr>
<tr>
<td>−</td>
<td>.</td>
</tr>
<tr>
<td>__</td>
<td>to</td>
</tr>
</tbody>
</table>

Table B.5: Special characters used in state names in GeNIe
Figure B.10: Bayesian Network for Wells-next-the-Sea with prior distributions
Figure B.11: Bayesian Network for Wells-next-the-Sea showing a 100 year return period event